## 數學系課程核心教材內容

| 課程名稱:(中文)數值常微分方程                               |   |      |      | 開課單位    | 應數碩博班 |
|--|---|------|------|---------|-------|
| (英文) Numerical Ordinary Differential Equations |   |      | 課程代碼 | 2105522 |       |
| 學分數  | 3 | 必/選修 | 選    | 開課年級    | 1     |

教學目標: This course focus on the analysis and algorithms for numerical approximations of differential equations. Students learn to identify the types of problems that require numerical techniques for their solutions. They also learn typical techniques for estimating error bounds for the approximations.

## 課程概述:

先修科目或先備能力:Differential Equations, Undergraduate Analysis

## 建議參考書目

- 1. Kindcaid & Cheney, "Numerical Analysis: Mathematics of Scientific Computing, 3<sup>rd</sup> ed., Brooks Cole, 2002
- 2. Bradie, A Friendly Introduction to Numerical Analysis, Pearson, 2006
- 3. Dormand, Numerical Methods for Differential Equations, CRC Press, 1996
- 4. Shampine, *Numerical Solutions of Ordinary Differential Equations*, Chapman & Hall,1994

## 課程大綱

| 單元主題  | 內容綱要   | 上課週數 |
|---|--|------|
| Computer Arithmetic*  | Floating-Point numbers and Roundoff error, Loss of Significance, Errors  | 1-2* |
| Solution of System of<br>Nonlinear Equations                | Bisection method, Newton's method, Secant method, Fixed point iteration, Horner's Algorithm  | 2-3  |
| Interpolation and Approximation                             | polynomial interpolation, Hermite interpolation, spline interpolation, B-splines*, best approximation*, orthogonal polynomials   | 3-4  |
| Numerical Differentiation and Integration                   | Richardson extrapolation, theory of Gaussian quadrature, Romberg integration, Euler-Maclaurin formula*   | 3    |
| Numerical Solution of<br>Ordinary Differential<br>Equations | Existence and uniqueness for IVP, Taylor-series method, Runge-Kutta and Runge-Kutta-Fehlberg methods, step-size control, dense output*, multistep methods, stability and stiffness, stiff solvers*, global error estimation*, shooting method for BVP* | 5-7  |

<sup>\*:</sup> optional